# CH 302 Spring 2007 Worksheet 7

For all of the problems on this worksheet, use the following K values:  $H_3PO_4$ :  $pK_{a1} = 2$   $pK_{a2} = 6$   $pK_{a3} = 10$  $H_2CO_3$ :  $pK_{a1} = 4$   $pK_{a2} = 10$ 

- 1. You drop 0.1 mol of KOH into 1 L of water. What is the pH of solution? Answer:  $pOH = -log[OH^-] = -log(C_b) = 1$  pH = 13
- 2. You drop 0.1 mol of KOH into a 1 L solution of 1 M  $H_3PO_4$  and  $KH_2PO_4$ . What is the pH of the solution?

Answer: Neutralize; you have 0.9 M H<sub>3</sub>A and 1.1 M H<sub>2</sub>A<sup>-</sup>.  $[H^+] = K_{a1}(C_a/C_b) = 10^{-2}(0.9/1.1) = 8.18 \times 10^{-3}$ pH = 2.09

**3.** You drop 0.1 mol of NaOH into a 1 L solution of 0.5 M RbHCO<sub>3</sub> and 0.5 M Na<sub>2</sub>CO<sub>3</sub>. What is the pH of the solution?

Answer: Neutralize; you have 0.4 M HA<sup>-</sup> and 0.6 M A<sup>2-</sup>.  $[H^+] = K_{a2}(C_a/C_b) = 10^{-10}(0.4/0.6) = 6.67 \text{ x } 10^{-11}$ pH = 10.18

4. You drop 0.5 mol of NaOH into a 1 L solution of 0.5 M RbHCO<sub>3</sub> and 0.5 M Na<sub>2</sub>CO<sub>3</sub>. What is the pH of the solution?

Answer: Neutralize; you have 1.0 M A<sup>2-</sup>.  $[OH^{-}] = (K_{b1}C_b)^{1/2} = [(K_w/K_{a2})C_b)^{1/2} = (10^{-4} \text{ x } 1.0)^{1/2} = 10^{-2}$ pOH = 2 pH = 12

You drop 1.0 mol of NaOH into a 1 L solution of 0.5 M RbHCO<sub>3</sub> and 0.5 M Na<sub>2</sub>CO<sub>3</sub>. What is the pH of the solution?
Answer: Neutralize; you have 1.5 M A<sup>2-</sup> and 0.5 M OH<sup>-</sup>.

**Answer:** Neutralize; you have 1.5 M A<sup>2</sup> and 0.5 M OH  $[OH^{-}] = C_b = 0.5 \text{ M}$  $pOH = 0.3 \qquad pH = 13.7$ 

For questions 6-13, 1.5 L 0.1 M H<sub>3</sub>PO<sub>4</sub> is titrated with 1 M NaOH. Give the pH for the given amount of NaOH solution added to the H<sub>3</sub>PO<sub>4</sub> solution.

	<b>V</b> <sub>NaOH</sub>	рН
6.	0 mL	$[H^+] = (K_{a1}C_a)^{1/2} = (10^{-2}x0.1)^{1/2} = 10^{-1.5}$
		pH = 1.5
7.	50 mL	Neutralize: 0.1 mol $H_3A$ and 0.05 mol $H_2A^2$ .
		$[H+] = K_{a1}(C_a/C_b) = 10^{-2}(0.1/0.05) = 2 \times 10^{-2}$
		pH = 1.7
8.	150 mL	Neutralize: 0.15 mol $H_2A^2$
		$[H^+] = (K_{a1}K_{a2})^{1/2} = (10^{-2}10^{-6})^{1/2} = 10^{-4}$
		$\mathbf{pH} = 4.0$
9.	250 mL	Neutralize: 0.05 mol $H_2A^2$ and 0.10 mol $HA^2^2$
		$[H^+] = K_{a2}(C_a/C_b) = 10^{-6}(0.05/0.10) = 5 \times 10^{-7}$
		$\mathbf{pH} = 6.3$

10.	300 mL	Neutralize: 0.15 mol HA <sup>2-</sup> [H <sup>+</sup> ] = $(K_{a2}K_{a3})^{1/2} = (10^{-6}10^{-10})^{1/2} = 10^{-8}$ <b>pH = 8.0</b>
11.	400 mL	Neutralize: 0.05 mol HA <sup>2-</sup> and 0.10 mol A <sup>3-</sup> [H <sup>+</sup> ] = K <sub>a3</sub> (C <sub>a</sub> /C <sub>b</sub> ) = $10^{-10}(0.05/0.10) = 5 \times 10^{-11}$ <b>pH = 10.3</b>
12.	450 mL	Neutralize: 0.15 mol $A^{2-}$ $K_{b1} = K_w/K_{a3} = 10^{-4}$ $C_b = (0.15 \text{ mol})/(1.5 \text{ L} + 0.450 \text{ L}) = 0.077 \text{ M}$ $[OH^-] = (K_{b1}C_b)^{1/2} = 2.8 \text{ x } 10^{-3}$ pOH = 2.6 <b>pH = 11.4</b>
13.	500 mL	Neutralize: 0.05 mol OH <sup>-</sup> and 0.15 mol A <sup>2-</sup> $C_b = (0.05 \text{ mol})/(1.5 \text{ L} + 0.5 \text{ L}) = 0.025 \text{ M}$ $pOH = -log[OH-] = -log(C_b) = 1.6$ pH = 12.4

14. Sketch the titration curve for a triprotic acid such as  $H_3PO_4$ .

**15.** Place the numbers 6 through 13 on the curve indicating the area of the titration curve corresponding to the calculation.



The 11 questions below represent the important areas of a triprotic acid titration curve. For each mixture, explain where you are on the curve after neutralization, provide the equation you would use for the calculation, and estimate the correct pH for the given mixture. DON'T USE A CALCULATOR. To guide you, draw the equilibrium species essential to determining the pH in the beaker provided (AFTER NEUTRALIZATION.) Hints: Assume there are no  $K_w$  contribution in the calculations use these numbers a lot: *Phosphoric acid values:*  $pKa_1 = 2$   $pKa_2 = 6$   $pKa_3 = 10$ 

 $H^+$ 

 $H^+$ 

## 16. 1M HCl and 1 M $H_3PO_4$

Where are you on a titration curve? Strong acid excess Equation used to determine the pH. C<sub>a</sub> Estimated pH. 0

#### 17. 1 M H<sub>3</sub>PO4

Where are you on a titration curve? Beginning of weak acid titration

Equation used to determine the pH.  $H^+ = (K_{al}C_a)^{0.5}$ 

Estimated pH. 1 (this is a bad approximation because K<sub>a1</sub> is so large)

## 18. 1M $H_3PO4$ and 1 M $NaH_2PO_4$

Where are you on a titration curve? First buffer region where  $pH = pK_1$ Equation used to determine the pH.  $H^+ = K_{a1}C_a/C_b$ Estimated pH. 2

# **19.** 1M H<sub>3</sub>PO4, 1 M NaH<sub>2</sub>PO<sub>4</sub> and .002M NaOH Where are you on a titration curve? First buffer region Equation used to determine the pH. $H^+ = K_{a1}C_a / C_b$ Estimated pH. Slightly more basic than pH 2



## 20. 1 M NaH<sub>2</sub>PO<sub>4</sub>







Where are you on a titration curve? First equivalence point Equation used to determine the pH.  $H^+ = (K_{a1}K_{a2})^{0.5}$  H Estimated pH. 4

## 21. 1 M $NaH_2PO_4$ and 1M $Li_2HPO_4$

Where are you on a titration curve? Second buffer region where  $pH = pK_2$ 

Equation used to determine the pH.  $H^+ = K_{a2}C_a/C_b$ 

Estimated pH. 6

## 22. 1 M NaH<sub>2</sub>PO<sub>4</sub>, Li<sub>2</sub>HPO<sub>4</sub> and 0.002 HCl

Where are you on a titration curve? Second buffer region Equation used to determine the pH.  $H^+ = K_{a2}C_a/C_b$ 

Estimated pH. Slightly more acidic than pH 6

## 23. 1M Li<sub>2</sub>HPO<sub>4</sub>

Where are you on a titration curve? Second equivalence point

Equation used to determine the pH.  $H^+ = (K_{a2}K_{a3})^{0.5}$ 

Estimated pH. 8

# 24. 1M Li<sub>2</sub>HPO<sub>4</sub> and 1M NaLiRbPO<sub>4</sub>

Where are you on a titration curve? Third buffer region where  $pH = pK_3$ 

Equation used to determine the pH.  $H^+ = K_{a3}C_a/C_b$ 

Estimated pH. 10











#### 25. 1M Li<sub>2</sub>HPO<sub>4</sub> and 1M NaLiRbPO<sub>4</sub> and .002M NaOH

Where are you on a titration curve? Third buffer region Equation used to determine the pH.  $H^+ = K_{a3}C_a/C_b$ Estimated pH. Slightly more basic than pH 10

## 26. 1M NaLiRbPO<sub>4</sub>

Where are you on a titration curve? Third equivalence point, all weak base Equation used to determine the pH.  $OH^- = (K_w/K_{a3}C_b)^{0.5}$ Estimated pH. 12

#### 27. 1M NaLiRbPO<sub>4</sub> and 1M NaOH

Where are you on a titration curve? Excess strong base

Equation used to determine the pH.  $C_b$ 

Estimated pH. 14





