

CH302 Worksheet 5 Answer Key: A charming calculator-free worksheet concerning  $K_{sp}$ ,  $K_w$ ,  $K_a$  &  $K_b$  and strong acids and bases.

1. Define  $K_{sp}$  for the dissolution of the following salts in water. If necessary, write a balanced chemical equation for the dissolution first.

- $\text{RbI}$ ,  $\text{RbI}(s) \rightleftharpoons \text{Rb}^+(aq) + \text{I}^-(aq)$ ,  $K_{sp} = [\text{Rb}^+][\text{I}^-]$
- $\text{Ca}(\text{NO}_3)_2$ ,  $K_{sp} = [\text{Ca}^{2+}][\text{NO}_3^-]^2$
- $\text{K}_3\text{PO}_4$ ,  $K_{sp} = [\text{K}^+]^3[\text{PO}_4^{3-}]$
- $\text{SrS}$ ,  $K_{sp} = [\text{Sr}^{2+}][\text{S}^{2-}]$
- $\text{Fe}_2(\text{SO}_4)_3$ ,  $K_{sp} = [\text{Fe}^{3+}]^2[\text{SO}_4^{2-}]^3$
- $\text{K}_3\text{Fe}(\text{C}_2\text{O}_4)_3$ ,  $K_{sp} = [\text{K}^+]^3[\text{Fe}^{3+}][\text{C}_2\text{O}_4^{2-}]^3$

2. Consider each of the salts below. Express each salt's molar solubility (we'll call it  $x$ ) in terms of  $K_{sp}$ . It might be useful to first write a balanced equation for each salt's dissolution and complete a RICE diagram.

- $\text{Cu}_3(\text{PO}_4)_2$ , molar solubility =  $x = (K_{sp}/108)^{1/5}$

R	$\text{Cu}_3(\text{PO}_4)_2(s)$	$\rightleftharpoons$	$3 \text{Cu}^{2+}(aq)$	+	$2 \text{PO}_4^{3-}(aq)$
I	~		0		0
C	~		+ 3x		+2x
E	~		3x		2x

$$K_{sp} = [\text{Cu}^{2+}]^3[\text{PO}_4^{3-}]^2 = (3x)^3 \cdot (2x)^2 = 108x^5$$

$$K_{sp} = 108x^5$$

$$x = (K_{sp}/108)^{1/5}$$

- $\text{MgSe}$ ,  $x = (K_{sp})^{1/2}$
- $\text{Li}_3\text{PO}_4$ ,  $x = (K_{sp}/27)^{1/4}$
- $\text{K}_3\text{Fe}(\text{C}_2\text{O}_4)_3$ ,  $x = (K_{sp}/729)^{1/7}$

3. Estimate the actual molar solubilities of the following salts in water based on their  $K_{sp}$  values.

- Barium Sulfate,  $\text{BaSO}_4$ ,  $K_{sp} = 1.08 \times 10^{-10}$ , molar solubility =  $x \approx 10^{-5} \text{ M}$
- Cadmium Phosphate,  $\text{Cd}_3(\text{PO}_4)_2$ ,  $K_{sp} = 2.53 \times 10^{-33}$ ,  $x \approx 10^{-6} \text{ M}$
- Lithium Carbonate,  $\text{Li}_2\text{CO}_3$ ,  $K_{sp} = 1.73 \times 10^{-3}$ ,  $x \approx 10^{-1} \text{ M}$
- Magnesium Ammonium Phosphate,  $\text{MgNH}_4\text{PO}_4$ ,  $K_{sp} = 2.5 \times 10^{-13}$ ,  $x \approx 10^{-4} \text{ M}$

4. Estimate the actual molar solubilities of the following salts in the following solutions based on the provided concentrations and  $K_{sp}$  values. It might be useful to first write a balanced equation for each salt's dissolution and complete a RICE diagram.

- Mercuric Bromide,  $\text{HgBr}_2$ ,  $K_{sp} = 8 \times 10^{-20}$ , in 2 M  $\text{Hg}(\text{NO}_3)_2$ , molar solubility =  $x = 10^{-10} \text{ M}$

R	$\text{HgBr}_2(s)$	$\rightleftharpoons$	$\text{Hg}^{2+}(aq)$	+	$\text{Br}^-(aq)$
I	~		2		0
C	~		+ x		+2x
E	~		2 + 3x		2x

$$K_{sp} = [\text{Hg}^{2+}][\text{Br}^-]^2$$

$$8 \times 10^{-20} = (2 + 3x) \cdot (2x)^2$$

For the term  $(2 + 3x)$ , it is safe to assume that  $2 + 3x \approx 2$ , and the equation reduces to

$$8 \times 10^{-20} = (2) \cdot (2x)^2$$

$$x = (8 \times 10^{-20}/8)^{1/2} = 10^{-10} \text{ M}$$

- Silver Chloride,  $\text{AgCl}$ ,  $K_{sp} = 1.56 \times 10^{-10}$ , in 15 M  $\text{KCl}$ ,  $x = 10^{-11} \text{ M}$
- Barium Iodate,  $\text{Ba}(\text{IO}_3)_2$ ,  $K_{sp} = 6.5 \times 10^{-10}$ , in 2.5 M  $\text{KIO}_3$ ,  $x = 10^{-10} \text{ M}$

5. Match the  $K_w$  values on the left with their corresponding pH values on the right. Assume you have a sample of completely pure water.

$K_w$ ( $e-14$ )	pH
0.114	7.08
0.293	7.27
0.681	6.14
1.008	6.92
1.471	7.47
2.916	6.63
5.476	7.00
51.3	6.77

6. Answer the following questions concerning the autoprotolysis of water;

a. Is the autoprotolysis of water endothermic or exothermic?

endothermic

b. What would be a simple experiment to verify this?

Measuring the pH of a sample of pure water at different temperatures - pH will be inversely proportional to temperature if autoprotolysis is endothermic.

c. What would be a simple way to calculate  $\Delta H_{\text{autoprotolysis}}$ ?

Similar to above, measuring pH at a range of temperatures would enable us to compute  $K_w$  at those temperatures and we could then use the van't Hoff equation.

7. List the 7 strong acids from memory.

Hydrochloric (HCl), Hydrobromic (HBr), Hydroiodic (HI), Sulfuric ( $H_2SO_4$ ), Nitric ( $HNO_3$ ), Chloric ( $HClO_3$ ) and Perchloric ( $HClO_4$ )

8. List the 8 strong bases from memory.

Lithium Hydroxide (LiOH), Sodium Hydroxide (NaOH), Potassium Hydroxide (KOH), Rubidium Hydroxide (RbOH), Cesium Hydroxide (CsOH), Calcium Hydroxide [ $Ca(OH)_2$ ], Strontium Hydroxide [ $Sr(OH)_2$ ], Barium Hydroxide [ $Ba(OH)_2$ ]

9. List the 14 spectator ions from memory. The answers to questions 7 and 8 are a **really** good starting point for this problem.

Chloride ( $Cl^-$ ), Bromide ( $Br^-$ ), Iodide ( $I^-$ ), Nitrate ( $NO_3^-$ ), Chlorate ( $ClO_3^-$ ), Perchlorate ( $ClO_4^-$ ), Lithium ion ( $Li^+$ ), Sodium ion ( $Na^+$ ), Potassium ion ( $K^+$ ), Rubidium ion ( $Rb^+$ ), Cesium ion ( $Ce^+$ ), Calcium ion ( $Ca^{2+}$ ), Strontium ion ( $Sr^{2+}$ ), Barium ion ( $Ba^{2+}$ )

10. Decide whether each of the species below is a weak acid or weak base. Note that it is possible to know this based on a chemical's name, and generally possible based on its formula.

a. pyridinium, weak acid

b. oxalate, weak base

c.  $HIO_3$ , weak acid

d.  $NH_3$ , weak base

- e. formic acid, **weak acid**
- f. hydrazine, **weak base**
- g.  $\text{ClO}^-$ , **weak base**
- h.  $\text{NH}_4^+$ , **weak acid**

11. Complete the following table: (Hint:  $-\log 0.4 = 0.4$ , this is a good and easy reference point to remember for the log function.)

	$[\text{H}^+]$ (M)	pH	$[\text{OH}^-]$ (M)	pOH
Solution A	0.4	0.4	$2.5 \times 10^{-14}$	13.6
Solution B	1	0	$10^{-14}$	14
Solution C	$10^{-13}$	13	0.1	1
Solution D	0.01	2	$10^{-12}$	12
Solution E	$10^{-15}$	15	10	-1
Solution F	$10^{-11}$	11	0.001	3
Solution G	$10^{-5}$	5	$10^{-9}$	9
Solution H	$2.5 \times 10^{-14}$	13.6	0.4	0.4
Solution I	$10^{-7}$	7	$10^{-7}$	7
Solution J	$10^{-9}$	9	$10^{-5}$	5

12. What would be the pH of the following solutions?

- a. 0.01 M  $\text{HClO}_4$ , **for a strong acid  $[\text{H}^+] = C_a$ ,  $-\log[\text{H}^+] = \text{pH} = 2$**
- b. 0.05 M  $\text{Ba}(\text{OH})_2$ , **note that some strong bases yield 2  $\text{OH}^-$ ,  $\text{pH} = 13$**
- c. 10 M  $\text{HNO}_3$ ,  **$\text{pH} = -1$**
- d. 10 M  $\text{LiOH}$ ,  **$\text{pH} = 15$**

13. What would be the pOH of the following solutions?

- a. 0.1 M  $\text{RbOH}$ , **for a strong base  $[\text{OH}^-] = C_b$ ,  $-\log[\text{OH}^-] = \text{pOH} = 1$**
- b. 0.5 M  $\text{Sr}(\text{OH})_2$ , **note that some strong bases yield 2  $\text{OH}^-$ ,  $\text{pOH} = 0$**
- c. 0.001 M  $\text{HClO}_3$ ,  **$\text{pOH} = 11$**
- d. 0.4 M  $\text{HI}$ ,  **$\text{pOH} = 13.6$**

14. What would be the pH of the following solutions? You may approximate if necessary; you should not need a calculator.

- a. 0.25 M  $\text{HNO}_2$ ,  $K_a = 4.0 \times 10^{-4}$ , **for a weak acid  $[\text{H}^+] = (K_a \cdot C_a)^{1/2}$ ,  $\text{pH} = 2$**
- b. 5.55 M  $\text{NH}_3$ ,  $K_b = 1.8 \times 10^{-5}$ , **for a weak base  $[\text{OH}^-] = (K_b \cdot C_b)^{1/2}$ ,  $\text{pH} = 12$**
- c. 0.0125 M ascorbic acid,  $K_a = 7.9 \times 10^{-5}$ ,  **$\text{pH} = 3$**
- d. 0.0135 M trimethylamine,  $K_b = 7.4 \times 10^{-5}$ ,  **$\text{pH} = 11$**
- e. 0.3 M  $\text{HOCl}$ ,  $K_a = 3.5 \times 10^{-8}$ ,  **$\text{pH} = 4$**

15. Consider each of the acids and bases below. Write the formula or name for each species' conjugate and calculate the  $K_a$  or  $K_b$  for that conjugate. Approximate if necessary.

- a. ammonium,  $K_a = 5.55 \times 10^{-10}$ , **ammonia,  $K_b = 1.80 \times 10^{-5}$**
- b.  $\text{OCl}^-$ ,  $K_b = 2.5 \times 10^{-7}$ ,  **$\text{HOCl}$ ,  $K_a = 4.0 \times 10^{-8}$**
- c. pyridine,  $K_b = 1.6 \times 10^{-9}$ , **pyridinium,  $K_a = 6.0 \times 10^{-6}$**
- d.  $\text{HCN}$ ,  $K_a = 4.0 \times 10^{-10}$ ,  **$\text{CN}^-$ ,  $K_b = 2.5 \times 10^{-5}$**

