

Worksheet 3 on Kinetics. Answer Key

1. Write the rate of the reaction $2\text{O}_3 \rightarrow 3\text{O}_2$ in terms of $\Delta[\text{O}_3]/\Delta t$.

$$-\frac{1}{2} \frac{\Delta[\text{O}_3]}{\Delta t}$$

2. Consider the following stoichiometric reaction: $2\text{A} + \text{B} \rightarrow \text{C} + \text{D}$

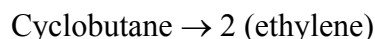
The reaction rates are measured with the following results:

Initial rate	$[\text{A}]_0$	$[\text{B}]_0$
1	2	1
2	4	1
1	2	2

What is the order of the reaction with respect to $[\text{B}]_0$?

Since we're looking at the order of $[\text{B}]_0$, all we have to look at where $[\text{B}]_0$ changes and where $[\text{A}]_0$ stays the same. You can see that $[\text{B}]_0$ doubles from the first row to the third row. However, the rate doesn't change, therefore the rate order is 0.

3. The first-order rate constant is $k = 3.4 \times 10^{-3} \text{ sec}^{-1}$ for the decomposition of cyclobutane and the half-life is 204 seconds.



What fraction of a sample of cyclobutane remains after 612 seconds under the specified conditions?

Time	Amount left (cyclobutane = C)
0	C
204	C/2
408	C/4
612	C/8

After 612 seconds, 1/8 of the original amount of cyclobutane is left.

4. The reaction $\text{A} + 3\text{B} \rightarrow \text{C} + 2\text{D}$ has a rate constant $k = 1.0 \times 10^{-5} \text{ sec}^{-1}$ at 27°C . If the activation energy for the reaction is 20,000 cal/mol, what is the value of the rate constant at 0°C ?

Explanation: Use the combined Arrhenius equation, $\ln \frac{k_2}{k_1} = (E_a/R) \left(\frac{1}{T_1} - \frac{1}{T_2} \right)$.

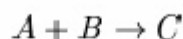
$$\ln \frac{k_2}{1e-5} = \left(\frac{20,000 \text{ cal/mol}}{1.987 \text{ cal/molK}} \right) \left(\frac{1}{300\text{K}} - \frac{1}{273\text{K}} \right)$$

$$k_2 = e^{\left[\left(\frac{20,000}{1.987} \right) \left(\frac{1}{300\text{K}} - \frac{1}{273\text{K}} \right) 1e-5 \right]}$$

$$= 3.6 \times 10^7$$

5.

The following data were collected for the following reaction at a particular temperature.



Three experiments give

Trial	Initial [A] M	Initial [B] M	Initial rate $\Delta[C]/\Delta t$ M/min
1	0.1	0.1	4.0×10^{-4}
2	0.2	0.2	3.2×10^{-3}
3	0.1	0.2	1.6×10^{-3}

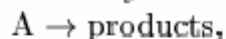
What is the rate law expression for this reaction?

$$0.4 \text{ M}^{-2} \text{ min}^{-1} [A][B]^2$$

See also: <http://neon.cm.utexas.edu/academic/courses/Spring2002/CH302/Laude/answers/e2key.pdf>

6.

A first order elementary reaction,



has a rate constant of $3.16 \times 10^8 \text{ sec}^{-1}$. At an instant in time, a concentration of $3.16 \times 10^{-6} \text{ M}$ of species A is created.

How long does it take for the concentration to fall by a factor of 4?

Solution:

$$\ln([A_0]/[A]) = akt$$

in this case, $a = 1$ and $k = 3.16\text{E}8$

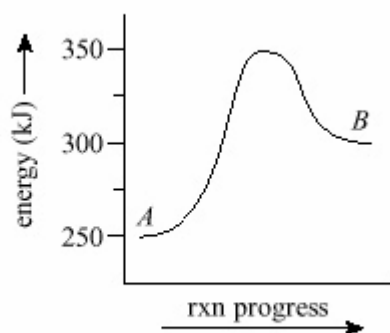
Since the concentration of A is decreasing by a factor of 4, $[A_0]/[A]$ is equal to 4.

$$\text{So, } \ln(4) = (1) * (3.16\text{E}8) * t$$

$$t = \ln(4)/3.16\text{E}8 = 4.38\text{E}-9 \text{ sec}$$

7.

Consider the potential energy diagram shown below.



What is the activation energy E_a for the reaction $A \rightarrow B$?

Solution:

We need to have enough energy to 'get to the top of the hill' in order to fall down to the products. So the energy must raise from 250 kJ (where A is) up to the top of the hill at 350 kJ. $350 - 250 = 100$ kJ